

# **Volumetric mesh creation using Delaunay tetrahedralization**

CS-116B: Computer Graphics Algorithms  
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# Volumetric mesh creation using Delaunay tetrahedralization

Two ways to represent a surface:

- Surface exterior is only represented.
- Surface exterior and interior is represented.

Representing both exterior and interior of a surface makes it easier to detect collisions between objects (especially objects that penetrate or collide with a surface).

# Volumetric mesh creation using Delaunay tetrahedralization

How to create a volumetric surface?

- Use a mass spring model with Delaunay tetrahedralization

Imagine a mesh comprised of tetrahedrons:

The edges of the tetrahedron are interconnected with invisible springs.  
The vertices of each tetrahedron contain a mass.

This is exactly like the 2D polygonal meshes we created with for cloth simulation in a Mass Spring model.

# Volumetric mesh creation using Delaunay tetrahedralization

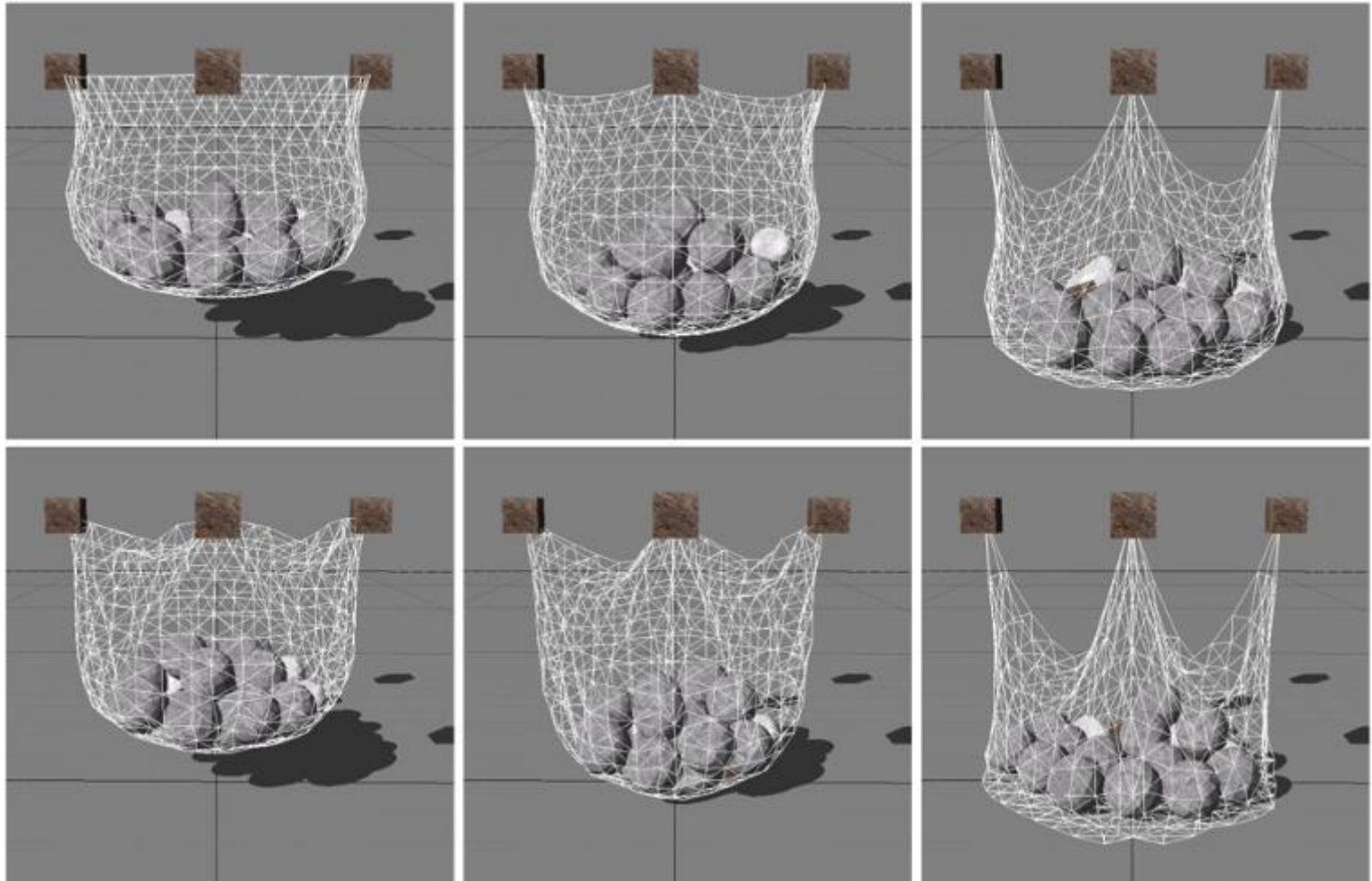
How do we implement a tetrahedral mesh?

“...we distribute a certain number of particles,  $p_i$ , evenly inside the volume defined by the surface mesh and on the surface mesh itself. To do this, we need an inside-outside test. The traditional way is to create a ray originating from the particle and count the number of surface triangle intersections. If the number is odd, the particle is inside the surface. This procedure requires the surface to be watertight. Then we run Delaunay tetrahedralization on these points and only keep tetrahedra with centers inside the surface” (p. 18).

# Procedure for volumetric mesh creation

1. create large tetrahedron that contains all points  $p_1, \dots, p_n$
2. **forall** points  $p_i$
3. clear face list  $l$
4. **forall** tetrahedra  $t_j$  the circumsphere of which contains  $p_i$
5. **forall** faces  $f_k$  of  $t_j$
6. **if**  $l$  contains  $f_k$  remove  $f_k$  from  $l$
7. **else** add  $f_k$  to  $l$
8. **endfor**
9. delete  $t_j$
10. **endfor**
11. **forall** faces  $f_k$  in  $l$
12. create a tetrahedron from  $f_k$  to  $p_i$
13. **endfor**
14. **endfor**
15. remove all tetrahedra that contain vertices of the large tetrahedron created in step (1)

# Simulating a cloth bag



Source: *Real Time Physics Class Notes*, p. 42